Subject Code: XXXXX Roll No:

BTECH (SEM-5) DESIGN AND ANALYSIS OF ALGORITHM 2021-22

TIME:3 HOUR Total Marks: 100

Instruction: Attempt the questions as per the given instructions. Assume missing data suitably.

SECTION - A Attempt All Parts in Brief 2*10 = 20<u>Q1</u> **Questions Marks** How analyze the performance of an algorithm in different cases? 2 (a) Derive the time complexity of merge sort. (b) (c) Explain left rotation in RB tree. (d) Write down the properties of Fibonacci Heap. 2 (e) Explain greedy programming in brief. 2 (f) What do you mean by convex hull? 2 (g) Write down the Floyd Warshal algorithm. 2 (h) Explain branch and bound method in brief. 2 (i) Explain randomized algorithm in brief. 2 (j) Explain NP-complete and NP-Hard. 2

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Attempt <u>Any Three</u> of the following	3*10 = 30
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Q2	Questions	Marks
(a)	Solve the recurrence i. $T(n) = 3T(n/4) + cn^2$ using recursion tree method. ii. $T(n) = n + 2T(n/2)$ using iteration method. (Given $T(1) = 1$)	10
(b)	What is Binomial Heap? Write down the algorithm for decrease key operation in Binomial Heap also write its time complexity.	10
(c)	Write and explain the Kruskal algorithm to find the Minimum Spanning Tree of a graph with suitable example.	10
(d)	What is N queens problem? Draw a state space tree for 4 queens problem using backtracking.	10

SECTION - C

Q3	Questions	Marks
(a)	Write merge sort algorithm and sort the following sequence {23, 11, 5, 15, 68, 31,4, 17} using merge sort.	10
(b)	What do you understand by stable and unstable sorting? Sort the following sequence {25, 57, 48, 36, 12, 91, 86, 32} using heap sort.	10
Q4	Questions	Marks
(a)	Discuss the various cases for insertion of key in red-black tree for given sequence of key in an empty red-black tree {15, 13, 12, 16, 19, 23, 5, 8}.	10
(b)	What is skip list? Explain the search operation in skip list with suitable example also write its algorithm.	10
Q5	Questions	Marks
(a)	What is Knapsack problem? Solve Fractional Knapsack problem using greedy programming for the following four items with their weights $w = \{3,5,9,5\}$ and values $P = \{45,30,45,10\}$ with Knapsack capacity is 16.	10
(b)	Write Clown the Bellman Ford algorithm to solve the single source shortest path problem also write its time complexity.	10
Q6	Questions	Marks

(a)	What is travelling Salesman Problem (TSP)? Find the solution of following TSP using branch and bound method.							10
		0	20	30	10	11		
		15	0	16	4	2		
		3	5	0	2	4		
		19	6	18	0	3		
		16	4	7	16	0		
(b)	Explain the method of finding Hamiltonian cycles in a graph using backtracking method with suitable example.						10	
Q7	Questions			Marks				
(a)	Write and explain the algorithm to solve vertex cover problem using approximation algorithm.				10			
(b)	Explain and write the Knuth-Morris-Pratt algorithm for pattern matching also write its time complexity.					10		